

```
In[596]:= ClearAll[m, x, γ, k, t, homogeneous, value1, value2, f3response, ν]
(*simple damped undriven harmonic oscillator*)
homogeneous = m x''[t] + γ x'[t] + k x[t] == 0
```

```
Out[597]= k x[t] + γ x'[t] + m x''[t] == 0
```

```
In[598]:= (*ansatz*)
x[t_] := x₀ E^{ν t}
```

```
(*solving for ν and plotting ν as a function of γ*)
homogeneous
```

```
f3response = Solve[homogeneous, ν]
value1 = ν /. f3response[[1]]
value2 = ν /. f3response[[2]]
f1[γ_] = Arg[value1]
f2[γ_] = value1
(*Plot[{f1[γ], f2[γ]}, {γ, 5}]*)
```

```
(*using the ansatz...*)
e^{t ν} k x₀ + e^{t ν} γ ν x₀ + e^{t ν} m ν² x₀ == 0
```

```
(*...solving for ν*)
```

$$\left\{ \left\{ \nu \rightarrow \frac{-\gamma - \sqrt{-4km + \gamma^2}}{2m} \right\}, \left\{ \nu \rightarrow \frac{-\gamma + \sqrt{-4km + \gamma^2}}{2m} \right\} \right\}$$

$$\sqrt{-4km + \gamma^2}$$

```
(*if γ > Sqrt[4km]: the real part of ν will make the system return to x==
0 without oscillation see detail on understanding complex...*)
```

```
(*if γ < Sqrt[4km]: the imaginary part of ν will make the system return to x==
0 with oscillation see detail on understanding complex...*)
```

```
In[410]:= (*understanding complex and real in  $\nu$  *)  
 $\nu = -.1 + I 1$  (* $\nu$  as a complex number*)  
 $p = 0$  (*phase shift*)
```

```
Plot[Re[E $\nu$  (t+p)], {t, 0, 50}]
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```
Out[410]= -0.1 + 1. i
```

```
Out[411]= 0
```

